

Error mitigation with Clifford quantum-circuit data

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- Quantum advantage and error mitigation.
- Clifford data regression (CDR) - arXiv:2005.10189.

Error mitigation with Clifford quantum-circuit data

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- Variable noise Clifford data regression (vnCDR) - arXiv:2011.01157.

Unified approach to data-driven quantum error mitigation

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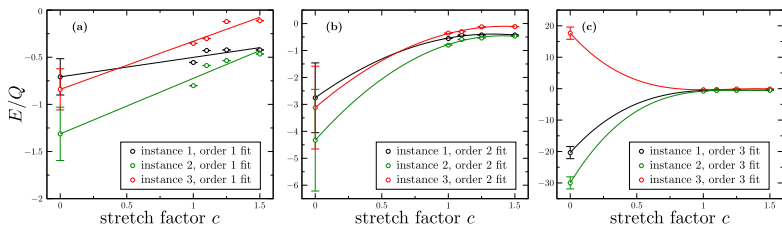
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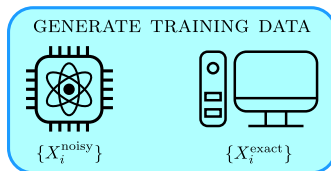
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- Fault-tolerant quantum computing is not possible with near-term (NISQ) quantum computers.
- Error mitigation methods reduce noise effects without performing full error correction.
- Error mitigation is expected to be necessary for quantum advantage with NISQ devices.
- Error mitigation for quantum advantage circuits is challenging.



- X - an observable of interest, $|\psi\rangle$ - a quantum circuit of interest.
- $X_\psi^{\text{exact}} = \langle \psi | X | \psi \rangle$, X_ψ^{noisy} - the noisy expectation value.

- 1 Choose near-Clifford classically simulable training circuits
 $\mathcal{S}_\psi = \{|\phi_i\rangle\}$.



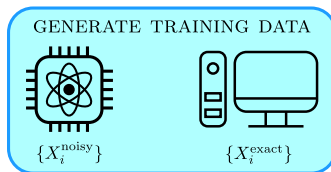
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- 2 Construct a training set

$$\mathcal{T}_\psi = \{X_{\phi_i}^{\text{noisy}}, X_{\phi_i}^{\text{exact}}\}.$$



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- 3 Learn a model for X^{exact} :

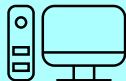
$$X^{\text{exact}} = a_1 X^{\text{noisy}} + a_2,$$

$$\operatorname{argmin}_{a_1, a_2} \sum_{\phi_i \in \mathcal{T}_\psi} (X_{\phi_i}^{\text{exact}} - a_1 X_{\phi_i}^{\text{noisy}} - a_2)^2.$$

GENERATE TRAINING DATA

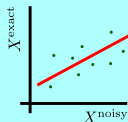


$\{X_i^{\text{noisy}}\}$



$\{X_i^{\text{exact}}\}$

LEARN TO CORRECT



Clifford Data Regression (CDR)

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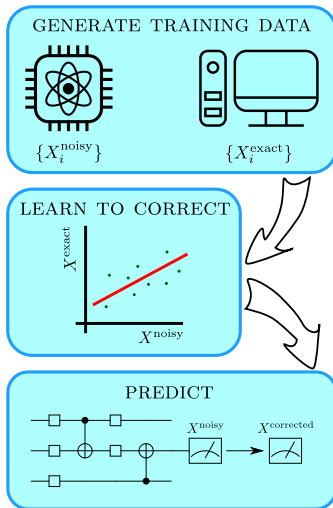
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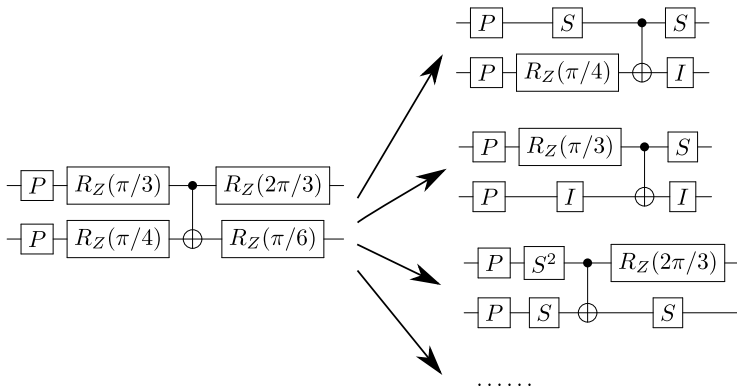
$$\operatorname{argmin}_{a_1, a_2} \sum_{\phi_i \in \mathcal{T}_\psi} (X_{\phi_i}^{\text{exact}} - a_1 X_{\phi_i}^{\text{noisy}} - a_2)^2.$$

- 4 Use the model to correct X_ψ^{noisy} .



- Near-Clifford circuits with up to $N \approx 50$ non-Clifford gates can be simulated classically.
- Replace non-Clifford gates by Clifford gates.
- An algorithm for IBM:

$$R_Z(\alpha) \rightarrow S^n, \quad S = R_Z(\pi/2), \quad n = 0, 1, 2, 3.$$



QAOA for the quantum Ising model

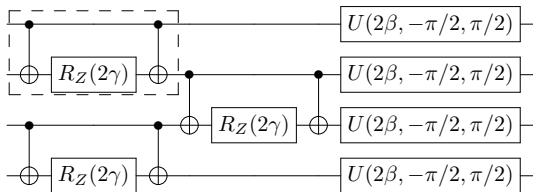
- The problem: Ground state simulation of a transverse-field 1D quantum Ising model ($g = 2$).

$$H = -g \sum_j \sigma_X^j - \sum_{\langle j,j' \rangle} \sigma_Z^j \sigma_Z^{j'}$$

- The QAOA (Quantum Alternating Operator Ansatz) ansatz:

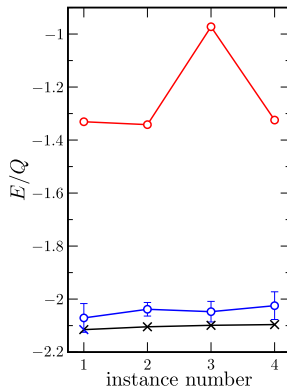
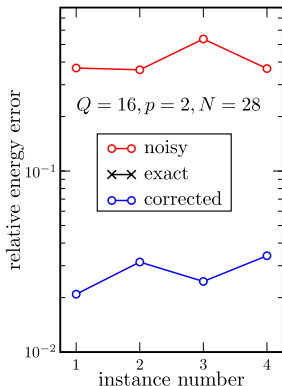
$$H = H_1 + H_2, \quad H_2 = -g \sum_j \sigma_X^j, \quad H_1 = - \sum_{\langle j,j' \rangle} \sigma_Z^j \sigma_Z^{j'}$$

$$|\psi(\beta_1, \gamma_1, \dots, \beta_p, \gamma_p)\rangle = \prod_{j=p, p-1, \dots, 1} e^{i\beta_j H_2} e^{i\gamma_j H_1} (|+\rangle)^{\otimes Q}, \quad |+\rangle = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle).$$

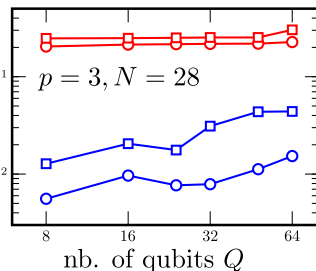
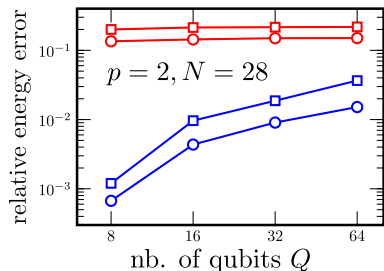
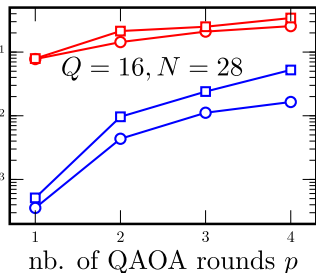
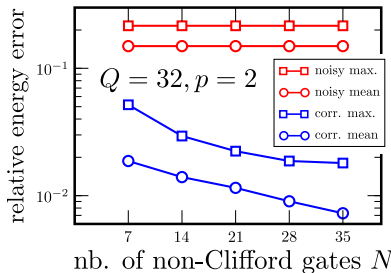


QAOA for the quantum Ising model - hardware implementation

- The QAOA is optimized with a noise model obtained by gate set tomography of IBM's Ourense quantum computer (L. Cincio, K. Rudinger, M. Sarovar, P. J. Coles, arXiv:2007.01210).
- Local minima of the optimization are simulated with IBM's Almaden quantum computer.
- A factor of 15 improvement obtained.



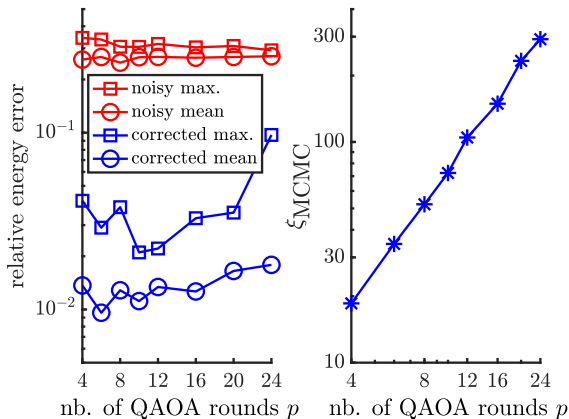
QAOA ground state simulation benchmark - scaling



At least a factor of 10 improvement obtained.

$$G^\alpha = \alpha G^{\text{noisy}} + (1 - \alpha) G^{\text{exact}} \quad \alpha = \frac{4}{p}$$

$$Q = 8, N = 28$$



At least a factor of 10 improvement up to $p = 24$.

Variable Noise Clifford Data Regression (vnCDR)

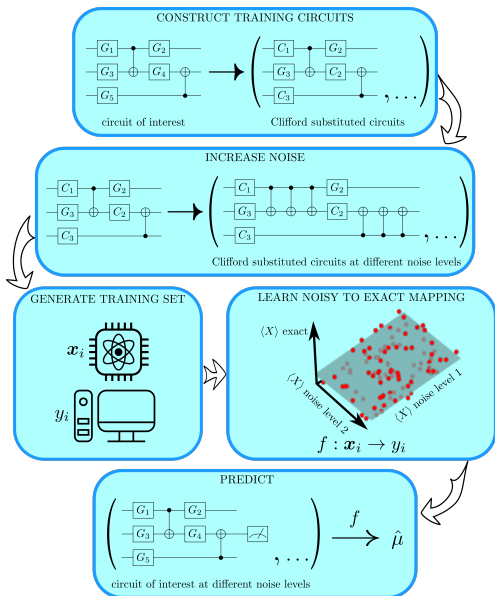
- 1 Choose training circuits as in the case of CDR.
- 2 Multiply noise level $j = 1, \dots, n$ as in the case of Zero Noise Extrapolation (ZNE).

- 3 Construct a training set $\mathcal{T}_\psi = \{X_{\phi_i}^{\text{noisy},j}, X_{\phi_i}^{\text{exact}}\}$.

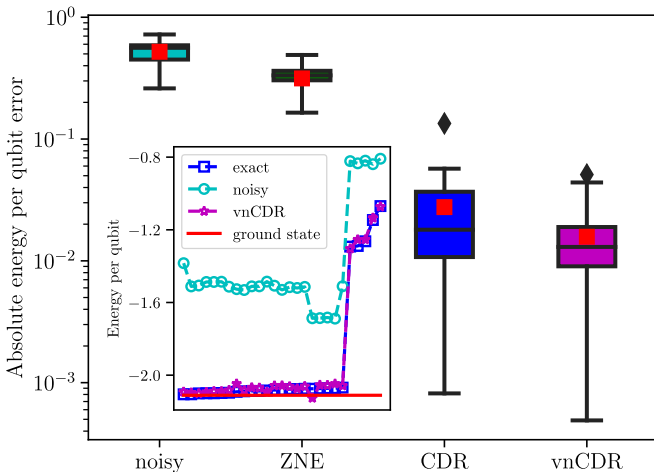
- 4 Learn a model for X^{exact} :

$$X^{\text{exact}} = \sum_j a_j X^{\text{noisy},j}.$$

- 5 Use the model to correct $X_\psi^{\text{noisy},j}$.

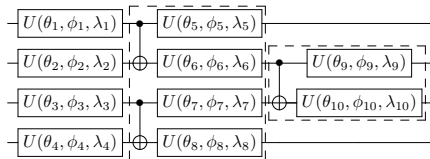


$$Q = 8, p = 4, N = 16$$

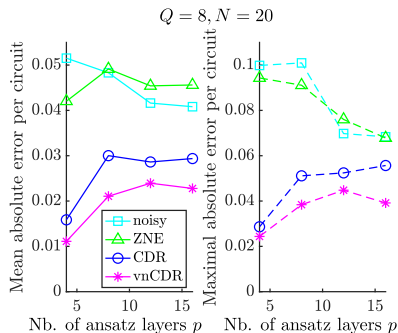
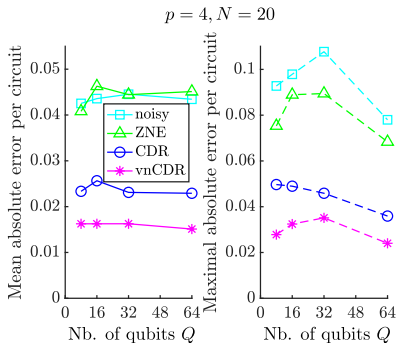


A factor of 33 improvement.

Random quantum circuits mitigation



$$U(\theta, \phi, \lambda) = R_Z(\phi + \pi)PR_Z(\theta + \pi)PR_Z(\lambda)$$



Systematic improvement over ZNE.

- Error mitigation methods based on learning the noise effects from classically simulable near-Clifford circuits.
- vnCDR unifies CDR and ZNE.
- Good scaling with with number of qubits.
- A factor of 10 improvement for the 16-qubit hardware QAOA implementation.
- A factor of 10 improvement for the 64-qubit QAOA implementation with realistic noise.
- Systematic improvement over ZNE.